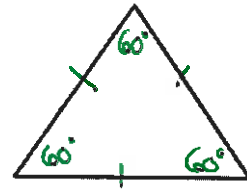


## Equilateral & Isosceles Triangles

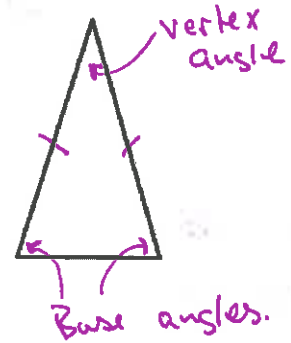
Equilateral Triangle:  $\Delta$  with 3  $\cong$  sides.

Theorem: Equilateral  $\Delta$  is also equiangular.

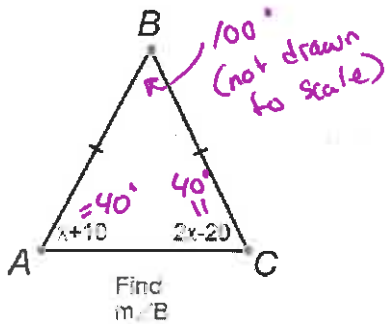


Isosceles Triangle:  $\Delta$  with 2  $\cong$  sides.

Theorem: Base  $\angle$ 's of an Isosc.  $\Delta$  are  $\cong$ .



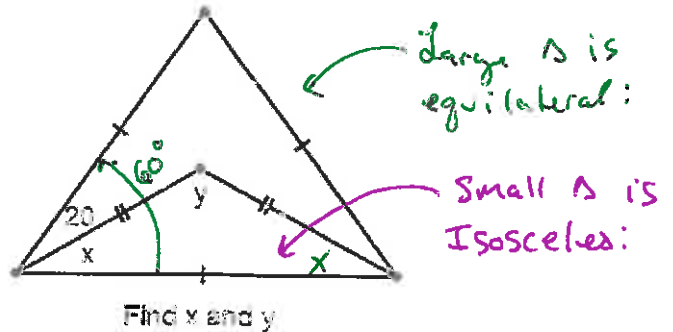
Examples:



$$x+10 = 2x-20$$

$$30 = x$$

$$m\angle B = 180 - 80 = 100^\circ$$



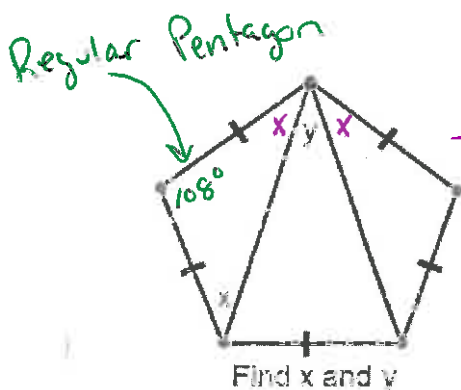
$$x+20 = 60$$

$$x = 40$$

$$x+x+y = 180$$

$$40+40+y = 180$$

$$y = 100^\circ$$



$$\text{int } \angle \text{ Sum} = 180(S-2)$$

$$= 180(3)$$

$$= 540^\circ$$

$$\text{each } \angle = \frac{540}{5} = 108^\circ$$

$$x+x+108 = 180$$

$$2x+108 = 180$$

$$2x = 72$$

$$\boxed{x = 36}$$

$$x+x+y = 108$$

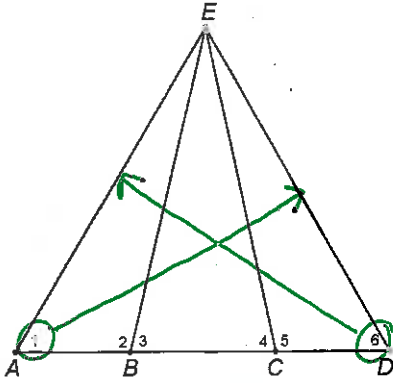
$$36+36+y = 108$$

$$72+y = 108$$

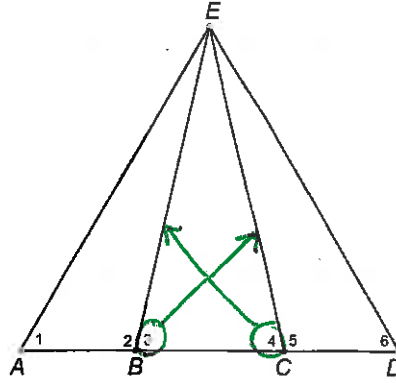
$$\boxed{y = 36}$$

**Isosceles Triangle Theorems:**

- In a  $\Delta$ , sides opp.  $\cong$   $\angle$ 's are  $\cong$
- In a  $\Delta$ ,  $\angle$ 's opp.  $\cong$  sides are  $\cong$

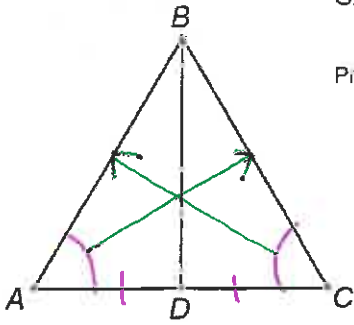


Given  $\angle 1 \cong \angle 6$   $\leftarrow$   $\angle$ 's in  $\Delta AED$   
 then  $\overline{AE} \cong \overline{ED}$



Given:  $\angle 3 \cong \angle 4$   $\leftarrow$   $\angle$ 's of  $\Delta BEC$   
 then:  $\overline{EB} \cong \overline{EC}$

**Example:**



SAS  
 (makes  $\Delta ABD \cong \Delta CBD$ )

Given:  $\angle A \cong \angle C$   
 D midpoint of  $\overline{AC}$

Prove:  $\angle ABD \cong \angle CBD$

*need to prove  $\cong$   $\Delta$ 's first.*

S	R.
① $\angle A \cong \angle C$ (angle)	① Given
② $\overline{AB} \cong \overline{BC}$ (side)	② In a $\Delta$ , Sides opp. $\cong$ $\angle$ 's are $\cong$ .
③ D midpt of $\overline{AC}$	③ Given
④ $\overline{AD} \cong \overline{CD}$ (side)	④ midpt makes $\cong$ segs.
⑤ $\Delta ABD \cong \Delta CBD$	⑤ SAS
⑥ $\angle ABD \cong \angle CBD$	⑥ CPCTC